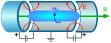
Neoclassical transport is enhanced flux across the magnetic field caused by symmetry-breaking

- · In non-neutral plasmas, these neoclassical fluxes are often the dominant plasma loss process
- 1. For known applied field errors that are not too big and do not produce localized particle trapping, experimentally observed radial particle transport is explained by the plateau regime
- To achieve accurate predictions precise self-consistent potentials must be calculated numerically, including finite length effects in realistic geometry. This was done using a new
- 3. Dependence of the transport on plasma length and magnetic field has been characterized for two types of errors: a potential asymmetry applied to a wall electrode, and a tilt of the magnetic field compared to the axis of the Penning trap
- 4. For shorter plasmas in strong B fields, plateau transport is strongly suppressed by a novel effect: a minimum axial bounce frequency exists in short plasmas that can be larger than the rotation frequency if B is large, suppressing bounce-rotation resonances
- 5. This effect also explains why spheroidal plasma equilibria have been observed to have lower

Nonneutral Plasmas have exceptional confinement properties, limited by neoclassical transport



ma" is confined by static electric and magnetic fields of a P Magnetic field is produced by a solenoid (not shown).

Axial confinement is due to electric fields from applied potentials on the end cylinders

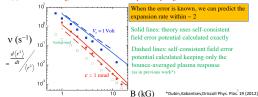
Radial confinement is due to the vxB force from plasma rotation. Typical rotation rates are $\frac{\omega_r}{2\pi} \sim 10\text{-}100 \text{ kHz}$

Confinement is limited by small field errors that break the cylindrical symmetry of the applied fields

These errors produce forces that torque on the plasma rotation ω_i , slowing it and reducing the confining vxB force. This causes plasma expansion and eventual loss to the walls

Experimental data (dots and squares) and 2 theories (solid & dashed lines) on radial expansion rate v versus B in electron plasma from three types of field errors:

- (a) unknown "background errors" in the trap fields
- (b) voltage $V_a \cos 2\theta$ applied to a single wall electrode, length 4cm, $V_a = 1$ Volt
- (c) a tilt of the magnetic field w.r.t. the trap axis by angle ε = 1 mrad



Fully Self-Consistent Calculation of **Neoclassical Transport in** Nonneutral Plasmas

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Ingredients in the theory: 1) Calculate realistic self-consistent plasma equilibrium for given measured radial density profile , assuming 1.0×10 $n_{_{0}}(r,z) = n_{_{0}}(r,0) \exp[-e(\phi_{_{0}}(r,z) - \phi_{_{0}}(r,0))/T];$ $\nabla^2\phi_0=4\pi\epsilon n_o(r,z)$

2) Using this equilibrium density and potential, solve for the radial flux from a small applied electrostation

a) "Brute force". Solve the linearized guiding center Fokker-Plank /Poisson system for the self-consister perturbed distribution function $\partial(r,z,y_s)$, assuming a uniform collision rate y. The perturbed distribution function is assumed to satisfy

 $\delta f \equiv (g - e\delta\phi/T)n_o f_$ where g is the non-adiabatic portion of the plasma response, which satisfies

$$v_z \frac{\partial g}{\partial z} - \frac{\partial \phi_0}{\partial z} \frac{\partial g}{\partial p_z} + \omega_E \frac{\partial g}{\partial \theta} + C(g) = \frac{\omega_F}{T} \frac{\partial \delta \phi}{\partial \theta},$$

 $\omega_E = \frac{c}{Br} \frac{\partial \phi_0}{\partial r}$: ExB rotation rate, $\omega_F = \omega_E - \frac{cT}{eBrn_c} \frac{\partial n_0}{\partial r}$: fluid rotation rate (incl. diamagnetic drift),

and
$$C(g) = \gamma \left(\frac{\partial^2 g}{\partial v_z^2} - \frac{mv_z}{T} \frac{\partial g}{\partial v_z} \right)$$
: Fokker Planck collisions

 $\delta \phi$ is determined self-consistently from δf : $\nabla^2 \delta \phi = -4\pi e \int dv \cdot \delta f$

radial flux is from
$$\theta$$
-averaged radial ExB drift: $\Gamma_r = \frac{c}{2\pi Br} \int d\theta dv$, $\delta f \frac{\partial \delta \phi}{\partial \theta}$

Solve this system iteratively on an $r_{e,v}$, $v_{e,v}$ grid: choose a $\delta \phi$, evaluate δf , reevaluate $\delta \phi$ via a relaxation algorithm, repeat)

b) Evaluate & directly in the plateau regime using action-angle variables appropriate to the plasma equilibrium The resulting flux should agree with method a) (it does!). The solid lines in the radial exp both method a and b: the difference between the methods is modifiable.

can then be solved analytically for a given perturbed potential

$$g = \sum_{a,j} e^{in\psi + il\theta} g_{a,j}(r, I), \quad \delta \phi(r, z, \theta) = \sum_{a,j} e^{in\psi + il\theta} \delta \phi_{a,j}(r, I)$$

$$\omega_{-}$$

$$\Rightarrow il \overline{\omega}_{E}(r, I)g_{n,i} + in\omega_{b}(r, I)g_{n,i} = il \frac{-r}{T} \delta \phi_{n,i}$$

$$\omega_{F} \quad l \delta \phi_{n,i}$$
(2)

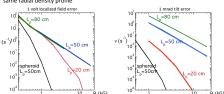
Take as the perturbed potential the output of the code from "brute force" method a). We do not try to iteratively Take as the perturbed potential the output of the coof for "brute force" method a). We do not try to iterative solve for a self-consistent g and $\delta \psi$ using the above expression. Divergence in g at bosone-rotation resonance are difficult to deal with, as are $(z,v) \mapsto (\psi,I)$ transformations at each rid g grid point. (The Plemel] formula can still be used to obtain the radial flux from the above expression for g.)

c) Redo method b) by determining $\delta\phi$ in a more approximate manner: Approximate δ' by it's bounce-averaged form in the collisionless Vlasov equation (the π - θ term in (*), which removes all bounce-notation resonances. Use this to calculate an approximate self-consistent perturbed potential $\delta\phi$ iteratively. Then use this approximate bounce-averaged form for $\delta\phi$ in plateau regime calculation b) or in a). This approximate method yields the

Radial Transport at different plasma lengths+for a spheroid

We varied the half-length L of the electrode structure: L=15 cm, L=30 cm(previous data) and L=45 cm, keeping the end electrodes at 100Volts and the radial density profile roughly the same. This makes cylindrical plasmas with three (full) lengths: Lp $^{-}$ 20 cm, Lp $^{-}$ 50 cm (previous), and Lp $^{-}$ 80 cm.

We also created a 50 cm long spheroid using a tailored $\,$ wall voltage, with roughly the same radial density profile



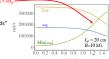
• At or below B~1 kG, transport from a localized error is roughly independent of plasma length, while transport from a tilt error scales



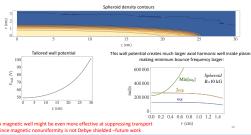
• Above B~1 kG, transport is suppressed at smaller Lo. For a spheroid it

Suppression of radial transport at smaller L_n and larger B

- Radial transport is dominated by flux at larger radii within the plasma.
- At these larger radii, and for shorter plasmas, the axial equilibrium electric field is not fully Debye shielded, making a weak harmonic axial potential well near z=0 (plasma axial center).
- This causes a minimum value of the axial bounce frequency $\min[\omega_b](r)$ at low particle kinetic energies
- For sufficiently large B, the plasma rotation frequency is reduced below this minimum. This suppresses bounce-rotation resonances at larger radii where Min(ω_c) > (ω̄_c
- This finite length effect is missed in previous work that uses periodic boundary conditions in z or "flat ends"



Suppression effect is even greater in spheroids



One experiment* also observed a reduced expansion rate when the plasma is confined in a harmonic potential in z (including plasma image charge effects)

